Automated Search for new Quantum Experiments

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Quantum mechanics predicts a number of, at first sight, counterintuitive phenomena. It therefore remains a question whether our intuition is the best way to find new experiments. Here, we report the development of the computer algorithm MELVIN which is able to find new experimental implementations for the creation and manipulation of complex quantum states. Indeed, the discovered experiments extensively use unfamiliar and asymmetric techniques which are challenging to understand intuitively. The results range from the first implementation of a high-dimensional Greenberger-Horne-Zeilinger state, to a vast variety of experiments for asymmetrically entangled quantum states—a feature that can only exist when both the number of involved parties and dimensions is larger than 2. Additionally, new types of high-dimensional transformations are found that perform cyclic operations. MELVIN autonomously learns from solutions for simpler systems, which significantly speeds up the discovery rate of more complex experiments. The ability to automate the design of a quantum experiment can be applied to many quantum systems and allows the physical realization of quantum states previously thought of only on paper.

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Quantum mechanics encompasses a wide range of counterintuitive phenomena such as teleportation [1,2], quantum interference [3], quantum erasure [4], and entanglement [5–10]. Despite our struggle to reconcile them with our picture of reality, these phenomena serve as building blocks for many exciting and useful quantum technologies such as quantum cryptography [11,12], computation [13,14], and metrology [15,16]. A significant challenge arises, however, when we try to combine such phenomena in order to perform a complex quantum task. Understanding the outcome of even a simple combination of these quantum building blocks can be daunting for the human intuition. Therefore, it is natural to ask: Given a certain desired property of a quantum system, what combination of quantum building blocks will be successful in achieving it?

In order to answer this question, we develop a classical computer algorithm called MELVIN, to which we teach how these quantum phenomena work and, subsequently, assign it a specific problem. The machine then takes on the task of finding and optimizing arrangements of quantum building blocks that result in a solution. This allows us to uncover experimental methods to create an array of new types of entangled states previously thought to exist only in theory. In addition, it also allows us to address the question of how to manipulate such high-dimensional quantum states, which is key for their use in quantum information systems.

While searching for these experiments, MELVIN enlarges its own toolbox by identifying useful groups of elements, leading to a significant speed-up in subsequent discoveries. The experiments found by our algorithm show a departure from conventional experiments in quantum mechanics in that they rely on highly unfamiliar, but perfectly conceivable experimental techniques. This provides some insight into the kind of out-of-the-box thinking that is required for creating such complex quantum states.

Our method aims to create and manipulate general complex quantum states for which arbitrary transformations are not known. The algorithm creates experiments using experimentally accessible optical components that can readily be implemented in the laboratory [17,18]. In addition, our algorithm considers multiple degrees of freedom of single quantum systems and can be extended to include nonlinear components and states more complex than single photons. This would allow us to investigate many other interesting quantum phenomena such as NOON states [19], induced coherence [20,21], quantum teleportation of more complex systems [2], or quantum metrology [15,16]. A complementary field is computer assisted or automated quantum circuit synthesis (QCS) [22–26], where optimal implementations for quantum algorithms are designed from universal sets of known quantum gates. While very powerful in its own right, the technique of QCS is used for linear qubit networks and usually requires fault-tolerant quantum computers for the implementation of its results.

The algorithm.—The main goal is to develop an algorithm which finds experimental implementations for quantum states or quantum transformations with interesting properties, see Fig. 1. Specific possible input states and a toolbox of experimentally known transformations utilizable by MELVIN are defined initially. Using the elements from the toolbox, the algorithm assembles new experiments by arranging elements randomly. Then, from the initial state,
For example, for the two-photon state $\psi = a[3] b[-3]$ (where $a$ and $b$ denote the input paths of the beam splitter), the beam splitter in path $a$ will lead to photon bunching, BS$[\psi, a, b] \rightarrow (a[-3] b[3]^{2})$, which is the well-known Hong-Ou-Mandel effect [3]. By realizing the calculations with symbolic algebra, adding new elements or even new degrees of freedom is very easy [27]. Furthermore, it allows easy human-readable intermediate forms, important for the examination of solutions and the novel techniques found by the algorithm.

Next, we demonstrate the working principles using two concrete examples. The demonstrations work in the regime of photonic quantum experiments, but the algorithm can readily be adapted to (a combination of) other systems such as cold atoms [28].

**Example 1: High-dimensional multipartite entanglement.**—The Greenberger-Horne-Zeilinger (GHZ) state is the most prominent example of nonclassical correlations between more than two involved parties and has led to new understanding of the fundamental properties of quantum physics [8]. It has been shown recently that its generalization to higher dimensions not only has curious properties [10], but that it is a limiting case of a much richer class of nonclassical correlations [9,29,30]. These new structures of multipartite high-dimensional entanglement are characterized by the Schmidt-rank vector and give rise to new phenomena that only exist if both the number of particles and the number of dimensions are larger than two. An example of a state with Schmidt-rank vector $4,2,2$ is the asymmetrically entangled state $|\psi_{4,2,2}\rangle = \frac{1}{2}(|0,0,0\rangle + |1,0,1\rangle + |2,1,0\rangle + |3,1,1\rangle)$. Here, the first particle is four-dimensionally entangled with the other two parties, whereas particle two and three are both only two-dimensionally entangled with the rest. This master-slave-slave configuration is one of the yet unexplored features that only exist in genuine high-dimensional multipartite entanglement and will be interesting to study in more detail in future. In order to make future experimental investigations possible, we aim to find high-dimensional multipartite entangled states in photonic systems.

Here, the initial state is created by a double spontaneous parametric down-conversion (SPDC) process. SPDC is a widespread source for the experimental generation of photon pairs. Multiple SPDC processes can be used to produce multipartite entanglement, as it is well known for the case of two-dimensional polarization entanglement [31,32]. However, instead of polarization, we use the OAM of photons [33–36], which is a discrete high-dimensional degree of freedom based on the spatial structure of the photonic wave function.

The experiments are generated using a set of basic elements consisting of beam splitters, mirrors, Dove prism, holograms, and OAM-parity sorters [27,37]. The holograms and the Dove prisms have discrete parameters corresponding to the OAM and phase added to the beam, respectively. These elements are randomly placed in one of six different paths (four of the paths are inputs of the two photon pairs and two are empty to increase variability).
One arm is used to trigger the tripartite state in the other three arms, which leads to roughly $10^{15}$ possible configurations. At the end, a postselection procedure consisting of the coincidence detection of four photons in the first four arms yields the final state.

We calculate the Schmidt-rank vector of the final state and select nontrivial ones (i.e., where there are no separable parties). Furthermore, for higher usefulness in experiments, we demand that the final state is maximally entangled in its orbital-angular-momentum. If the criteria hold, the experiment is reported.

**Example 2: High-dimensional cyclic operations and learning.**—In the second example, we are interested in high-dimensional cyclic rotations, which are special cases of high-dimensional unitary transformations. A set of states is transformed in such a way that the last element of the set transforms to the first element (for example, $|1\rangle \rightarrow |2\rangle \rightarrow |3\rangle \rightarrow |1\rangle$ is a three cycle). Such transformations are required in novel kinds of high-dimensional quantum information protocols [38,39] as well as in the creation of high-dimensional Bell states. Here, our input is a set of high-dimensional states encoded in different degrees of freedom (path, polarization, and OAM). While the creation and verification of high-dimensional entanglement in OAM is well known [35,36], the knowledge of how to perform arbitrary transformations in this degree of freedom is still lacking. Thus, finding such transformations in OAM is very important, as it would enable practical experiments with high-dimensional quantum states.---

FIG. 2. Experimental implementations of high-dimensional multipartite entangled quantum states. (a) The experimental implementation for a three-dimensional three-partite GHZ state. If detector $T$ (Trigger) observes a photon in the state $|T\rangle = |(0) + (1)\rangle$, then the rest of the quantum state is in a GHZ state, which looks like $|\psi\rangle = |0, 0, 0\rangle + |1, 1, 1\rangle + |2, 2, 2\rangle$ (up to local transformations). The parity sorter, as described in [37], can sort even and odd OAM modes. The three-dimensional GHZ state has a Schmidt-rank vector of $(3, 3, 3)$ (all components are symmetrically entangled with the rest of the state). (b) A more complex experiment is required for higher-order Schmidt-rank vectors. The $(10, 6, 5)$ state is one example of asymmetrically entangled quantum states. The experiments are just two examples of 51 implementations found for creating a variety of different entangled states.
quantum states and find application in high-dimensional quantum information protocols.

The experiments are generated using a set of basic elements that consists of polarizing and nonpolarizing beam splitters, Dove prisms, mirrors, holograms, and half-wave plates. These elements are placed in one of three different splitters, Dove prisms, mirrors, holograms, and half-wave elements that consists of polarizing and nonpolarizing beam quantum information protocols.

The criterion is based on the largest cycle of the transformation: A number of input states [with different polarization (horizontal and vertical), OAM (ℓ = −10 to +10) and paths] are calculated. Then, we search subsets of modes that are transformed in a closed cycle, as described above, and select the largest closed cycle. MELVIN was able to find the first experimentally realizable OAM-only four-cyclic transformation, OAM-polarization hybrid three-, six-, and eight-cyclic rotations and up to 14-cyclic rotations using OAM, polarization, and path (Fig. 3 and [27]).

Complex problems can be solved more efficiently by reusing solutions to simpler problems [40,41]: Whenever MELVIN finds a solution for a simpler system, it memorizes the experimental configuration as a new part of its initial toolbox [27]. The novel elements in the toolbox can be used to construct the next experimental configuration. To compare the effectiveness of learning, we analyze the algorithm with and without the ability to increase its own possible experimental configurations.

The experiments for three-cyclic and eight-cyclic transformations were not found (within 250 hours) without learning, while experiments for four-cyclic and six-cyclic rotation were found three and four times in 250 hours, respectively. The errors stand for 1 standard deviation, calculated from the times it took to find the solution. Thus, autonomously extending the set of useful transformations improves MELVIN’s performance, which is crucial for scaling to more complex experiments.

Conclusion and outlook.—We have shown how a computer can find new quantum experiments. The large number of discoveries reveals a way to investigate new families of complex entangled quantum systems in the laboratory. Several of these experiments are being built at the moment in our labs [17, 18]. In contrast to human designers of experiments, MELVIN does not follow intuitive reasoning about the physical system and, therefore, leads to the utilization of many unfamiliar and unconventional techniques that are challenging to understand. The algorithm can learn from experience (i.e., previous successful solutions), which leads to a significant speed-up in discoveries of more complex experiments.

MELVIN can be applied to many other questions about the creation and manipulation of quantum systems, such as the search for more general high-dimensional transformations with different degrees of freedom and for different physical systems such as ultracold atoms [28] or for efficient generation of other types of important quantum systems such as NOON states [19]. In order to improve the efficiency of finding solutions, powerful techniques from artificial intelligence research can be applied, such as evolutionary algorithms [42] (where the experiment and the resulting quantum state play the role of genotype and phenotype, respectively), reinforcement learning techniques [41,43,44] (by implementing a reward function depending on the closeness of the quantum states properties to the desired properties), or
entropy-based [45] and big-data methods [46] (in order to find more unexpected solutions).

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